Abstract

The last chapter of Horn (1972) outlines an asymmetry in lexicalization potential for values situated on the square of opposition—in its simplest form, the contrast between no(ne) as the contradictory of some vs. *nall as the contradictory of all—and offers a Gricean program to account for this asymmetry. In this paper, I return to the scene of the crime, including a (not entirely impartial) review of proto-Gricean approaches to the three-sided square dating back to De Morgan (1858) and a defense of the pragmatic line against critiques dismissing it as inadequate or flawed by Hoeksema 2003, Jaspers 2005, Seuren 2006, inter al.) on the three-sided square.

I argue that the arguments for a Gricean approach have not been fully appreciated, including those based on (i) the relation between the square and quantity scales (Horn 1989) as exemplified across quantifiers, modals, and binary connectives, (ii) the status of the “intermediate” values on the square (e.g. most/many/few for the determiners; likely/unlikely for the epistemic modalities; should/ought to/shouldn’t for the modal auxiliaries, usually/often/rarely for the quantificational adverbs, etc.) and their implications for a predictive model of lexicalization, and (iii) the widespread cross-linguistic tendency to minimize the expression of subcontrary opposition and maximize that of contrary opposition in natural language as attested by pragmatic strengthening implicatures (as in “neg-raising”) and O>E drift, as in the contrary (=NECESSARY [NOT])] reading expressed by Fr. “Il ne faut pas que tu meures.”
The back cover blurb for Dany Jaspers’ (2005) masterful treatise on the linguistic asymmetry of the Square of Opposition begins as follows:

*Operators in the Lexicon* begins with an old chestnut: why are there no natural single word lexicalizations for negations of the propositional operator *and* and the predicate calculus operator *all*: neither *nand* nor *nall*?

I assume that the “old chestnut” in question concerns not senses 1–5 of the *American Heritage Dictionary* entry (http://dictionary.reference.com/browse/Chestnut) for *chestnut* – relating to trees of the genus *Castanea*, their wood or nuts, the reddish-brown color of those trees or the horse of the same color, or a callus on a horse’s foreleg –but rather sense 6: ‘An old, frequently repeated joke, story, or song.’ Given the limitations of the prose medium, I will assume the intended reference can be further narrowed to the second of the three disjuncts within sense 6, and in particular to the frequently recited story I shall describe (with apologies to the soi-disant Réage 1954) as *l’Histoire d’*O:

In a wide variety of languages, values mapping onto the southeast, O vertex of the Square of Opposition are systematically restricted in their potential for lexicalization or direct expression; this asymmetry is attributable to the scalar implicature relation obtaining between the two subcontraries.


The path between the I and O subcontraries *some* and *some not* (or *not all*) has proved to be a long and winding road. On the minority view, *some* is two-sided, with upper as well as lower bound, and is thus incompatible with *all*. Some have wishfully read this position into Aristotle –

On the Aristotelian theory…wherever the affirmative “some are” applies, the negative proposition “some are not” holds also.

(Dewey 1938: 182)

Aristotle seems to think that the main function of a particular statement is to describe a situation where the corresponding universal statement is false. His reasoning seems to be: If the universal is true, why assert the particular?

(Rose 1968: 41)

But such a reading is not tenable, given Aristotle’s observation on the nature of the relation between the two subcontraries themselves (“Verbally four kinds of opposition are possible…but really there are only three: for the particular affirmative is only verbally opposed to the particular negative” – *Prior Analytics I, 63b21 ff.*) and his explicit endorsement of the one-way subaltern entailment from A to I and from E to O:
For having shown that it belongs to all, we will have shown also that it belongs to some; similarly, if we should show that it belongs to none, we will have shown also that it does not belong to all.
(Aristotle, *Topics* 109a3)

Most commentators concur; in the words of the great Arab philosopher Avicenna (ibn-Sīnā):

If you say “some men are so-and-so”, it is not necessary that some others are not so-and-so. If the proposition is about all, it is also about some.
(Zabeeh 1971: 24)

But even if Aristotle did not support a two-sided *some*, others did. Priority may belong to the early 6th century Buddhist logician Dignāga and his colleagues who, in their *hetu-cakra* or Wheel of Reasons,

...do not admit four kinds of proposition like Aristotle and the Scholastics, but only three, since they interpret ‘Some S is P’ not as ‘at least some’ but as ‘at least some and not all’...This would give a logical triangle in place of the western logical square.
(Bochenski 1961: §53E; cf. Tucci 1928)

Such triangles of opposition did not surface explicitly in the West until the mid-19th century when Sir William Hamilton of Edinburgh inaugurated a debate over the proper treatment of the subcontraries. Distinguishing two senses of *some*, the INDEFINITE (*at least some*) and the SEMI-DEFINITE (*some but not all*), Hamilton (1860: 254) regarded the latter as basic: ‘Some, if not otherwise qualified, means *some only* –this by presumption.’ On this reading of the particular, the two statements *Some men are learned* and *Some men are not learned* are not only (as for Aristotle) compatible, given that their conjunction is consistent, but logically indistinct. The purported opposition between the two subcontraries, charged Hamilton (1860: 261), was ‘only laid down from a love of symmetry, in order to make out the opposition of all the corners in the square of opposition...In reality and in thought, every quantity is necessarily either all, or none, or some. Of these the third...is formally exclusive of the other two.’

As was his wont, Augustus de Morgan was unimpressed with his rival’s stance, although he did concede the existence of what we would now view as pragmatic upper-bounding. Some sample passages (here and below, emphasis is added):
In common conversation the affirmation of a part is meant to imply the denial of the remainder. Thus, by ‘some of the apples are ripe’, it is always intended to signify that some are not ripe.

(De Morgan 1847: 4)

Some, in logic, means one or more, it may be all. He who says that some are, is not held to mean the rest are not. ‘Some men breathe’…would be held false in common language [which] usually adopts the complex particular proposition and implies that some are not in saying that some are.

(De Morgan 1847: 56)

With logicians the word some has in all time been no more than a synonym of not–none: it has stood for one or more, possibly all. With the world at large it is sometimes possibly all, sometimes certainly not all, according to the matter spoken of. But with the logician “some are” is merely and no more than the contradictory of “none are”…Some equally contains some–certainly–not–all and some–possibly–all.

(De Morgan 1861: 51)

As recognized by both De Morgan and Mill (another captain of the anti-Hamiltonian troops), the possibility of upper bounding is subject not only to the vagaries of context and speech level but more specifically to the relative epistemic insecurity of the speaker:

There are three ways in which one extent may be related to another…: complete inclusion, partial inclusion with partial exclusion, and complete exclusion. This trichotomy would have ruled the forms of logic, if human knowledge had been more definite…As it is, we know well the grounds on which predication is not a trichotomy, but two separate dichotomies.

(De Morgan 1858: 121)

No shadow of justification is shown…for adopting into logic a mere sous-entendu of common conversation in its most unprecise form. If I say to any one, “I saw some of your children today”, he might be justified in inferring that I did not see them all, not because the words mean it, but because, if I had seen them all, it is most likely that I should have said so: even though this cannot be presumed unless it is presupposed that I must have known whether the children I saw were all or not.

(Mill 1867: 501)

In such remarks, De Morgan and Mill prefigure the two-stage quantity implicature procedure of (neo-)Gricean pragmatics: The use of a weaker value (e.g. some, most) suggests that for all the speaker knows any stronger value—and especially the strongest value—on the same scale (all) could not have been substituted salva veritate. Speaker a’s utterance of …W… implicates not Kₐ¬(S), i.e. that a knows that the stronger counterpart …S… is false, but only (ceteris paribus) that ¬Kₐ(S). The strengthening of ¬Kₐ(S)
to K,¬(S) is possible only given what Geurts (2009) calls the “competence assumption” (cf. also Horn 2009: §2).

Mill’s proto-Gricean allusion to a tacit principle mandating the speaker to use the stronger all in place of the weaker some when possible, while inviting the hearer to draw the corresponding inference when the stronger term is not used, is echoed even by one of Hamilton’s sometime supporters:

Whenever we think of the class as a whole, we should employ the term All; and therefore when we employ the term Some, it is implied that we are not thinking of the whole, but of a part as distinguished from the whole –that is, of a part only.

(Monck 1881: 156)

The idea that some should be assigned a two-sided meaning rather than, or along with, the traditional one-sided interpretation did not die with Hamilton. Ginzberg (1913, 1914) carried the quarrel across the Channel, jetisoning the square of opposition for a triangle of contraries with vertices representing all, none, and exactly some –‘quelques et rien que quelques’. But Couturat (1913, 1914), only too eager to play De Morgan to Ginzberg’s Hamilton, sought to dissuade his countryman from following ‘le plus mauvais des logiciens’ in collapsing the two distinct subcontraries into one basic proposition which is in fact a logical conjunction; he argues that the classical system cannot be perfected by adopting ‘précisions’ that are inconsistent with its very spirit.

John Neville Keynes echoed Mill in observing (1906: 202–3) that a speaker whose knowledge is incomplete cannot use some S’s are P with the meaning ‘some only’. Unfortunately, many logicians “have not recognized the pitfalls surrounding the use of some. Many passages might be quoted in which they distinctly adopt the meaning –some, but not all.”

To which the great Danish linguist Jespersen (1924: 324) retorted “in the name of common sense”, why do logicians “dig such pitfalls for their fellow-logicians to fall in”? Jespersen consequently proselytizes for the “tripartition” of operators in (1) (cf. De Morgan’s functional “trichotomy” above) and implicitly proposes his own Triangle of Opposition (1917: Chapter 8) as indicated in (2)

(1) A: all
     B: some/a
     C: none/no

everybody
somebody
nobody
always
sometimes
never
everywhere
somewhere
nowhere
A: necessity    must/need    command
B: possibility  can/may     permission
C: impossibility cannot    prohibition

The effect, as with Ginzberg (or Dignāga), is to triangulate the Square:

(2)

Figure 1

But while Jespersen’s B category, the nadir of his Triangle, represents a semantic conjunction (or neutralization) of the I and O vertices of the traditional Square, it has the lexical membership of the I vertex (*some, possible*). On logical, epistemological, and discourse grounds the identification of I and O is ultimately untenable, precisely for the traditional reason that the former provides the contradictory of E, the latter of A. (See Horn 1973 for more on these debates in the light of neo-Gricean pragmatics.)

With characteristic insight, Sapir (1930: 21) opted for a solution midway between the classical Square and the Jespersenian Triangle. His particular subcontraries are neither semantically bilateral nor strictly unilateral. (Again, emphasis is added.)

‘Not everybody came’ **does not mean** ‘some came’, **which is implied**, but ‘some did not come’. **Logically**, the negated totalizer *not every* should include the totalized negative, i.e. opposite or contrary *none*, as a possibility, but **ordinarily** this interpretation is excluded.
Note especially Sapir’s use of *is implied* (vs. *means*) and his qualifier *ordinarily*, emphasizing the essential role of the context in licensing the implication in question.

An expanded development of the triangle was launched in the early 1950’s, appropriately enough by three philosophers working independently but exploiting essentially the same geometry. For Jacoby (1950), Sesmat (1951), and especially Blanché (1952, 1953, 1969), the square and triangle in (4) can be combined to form a Hexagon of Opposition on which the diametrically opposed terms are contradictories:\footnote{It will be noticed that Sesmat’s hexagon has the Y above and the U below, as does the somewhat sketchier model of Hegenberg (1957). I opt here for Blanché’s vowel system for its mnemonic value, the IOU serving to acknowledge the incurring of an informational debt. Von Wright (1951) presupposes a logical pentagon, with a nadir (= our Y) for the conjunction of I and O but no apex (= U) for its contradictory, as in (8) below.}
In earlier work (Horn 1990), I suggested reconfiguring the hexagons in (3) as a Logical Star of David, in which the triple of pairwise contraries \(<A\ E\ Y>\) (exactly one of which must be true in any context) is superimposed on the triple of pairwise subcontraries \(<I\ O\ U>\) (exactly one of which must always be false).
The (neo-)Gricean approach derives the relationship between the subcontraries by means of a pragmatic principle variously defined in terms of strength or quantity:

One should not make the (logically) lesser, when one could truthfully (and with greater or equal clarity) make the greater claim.
(Strawson 1952: 178–9, with acknowledgments to ‘Mr H. P. Grice’)

One should not make a weaker statement rather than a stronger one unless there is a good reason for so doing.
(Grice’s own ‘first shot’, 1961: 132)

Make your contribution as informative as is required (for the current purposes of the talk-exchange).
(Grice’s first maxim of quantity [1967] 1989: 26)

Make the strongest possible claim that you can legitimately defend!
(Fogelin’s rule of strength, 1967: 20)

This was clearly an idea whose time had come. The Fogelin (1967: 20–22) “rule of strength” is devised contemporaneously with Grice’s William James lectures and generates a set of rules of use for the subcontraries:

(6) (i) Do not employ an I or an O proposition in a context where you can legitimately employ an A or an E proposition...The use of one sub-contrary typically suggests the appropriateness of using the other.
(ii) Do not affirm one subcontrary if you are willing to deny the other.
(iii) Subcontraries tend to collapse together.

Based on the rules, Fogelin tries his hand at beating Squares into Triangles:

![Figure 4]

But Fogelin’s triangles – unlike those of the Dignāga-Jespersen-Jacoby-Sesmat-Blanché tradition(s) – are pragmatically derived and not semantically driven. The move from I and O to their conjunction Y, as in the pentagonalized Square in (8), is context dependent; it is not that the subcontraries are equipollent but that they will tend (ceteris paribus) to result in a speaker’s communicating the same state of affairs.
(8) Extended Square of Opposition

In fact, it can be argued that what we need is not so much a triangle or a pentagon as a defective three-cornered square, given that in a wide variety of languages those values mapping onto the southeast corner of the Square are systematically restricted in their potential for lexicalization. This crucial asymmetry was perhaps first recognized by St. Thomas Aquinas, who observed that whereas in the case of the universal negative (A) “the word ‘no’ [nullus] has been devised [sic!] to signify that the predicate is removed

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2 Cf. Horn 1989: 252–53 for elaboration. I pass over another issue arising in the mapping of quantificational values onto the Square: the role of existential import. Which (if any) of the four statement forms entail or presuppose that the set over which the quantifier ranges is non-null and how does this affect the subaltern and other relations? In particular, if (as in the modern tradition) all is import-free while some is not, does this vitiate the Square, as Fogelin (1978) maintains? The fact that other operators (binary connectives, adverbs, modals, deontics), for which existential import is irrelevant, can be mapped onto the Square makes Fogelin’s move as unappealing as it is unnecessary. This leaves a number of options open for dealing with questions of import and quantification and their relation to the Square; see Horn (1997) for elaboration.
from the universal subject according to the whole of what is contained under it”, when it comes to the particular negative (O), we find that


there is no designated word, but ‘not all’ \([\text{non omnis}]\) can be used. Just as ‘no’ removes universally, for it signifies the same thing as if we were to say ‘not any’ [i.e. ‘not some’], so also ‘not all’ removes particularly inasmuch as it excludes universal affirmation. (Aquinas, *in Arist. de Int.*, Lesson X, Oesterle 1962: 82–3)

Thus alongside the quantificational determiners *all, some, no*, we never find an O determiner *nall*; corresponding to the quantificational adverbs *always, sometimes, never*, we have no *nalways (= ‘not always’, ‘sometimes not’). We may have univerbations for *both (of them), one (of them), neither (of them)*, but never for *noth (of them) (= ‘not both’, ‘at least one…not’); we can find connectives corresponding to *and, or, and sometimes nor (= ‘and not’), but never to *nand (= ‘or not’, ‘not…and’). Schematically:

<table>
<thead>
<tr>
<th>DETERMINERS/QUANTIFIERS</th>
<th>QUANT. ADVERBS</th>
<th>BINARY QUANTIFIERS</th>
<th>CORRELATIVE CONJUNCTIONS</th>
<th>BINARY CONNECTIVES</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>A:</strong> all (\alpha), everyone</td>
<td>always</td>
<td>both (of them)</td>
<td>both…and</td>
<td>and</td>
</tr>
<tr>
<td><strong>I:</strong> some (\alpha), someone</td>
<td>sometimes</td>
<td>one (of them)</td>
<td>either…or</td>
<td>or</td>
</tr>
<tr>
<td><strong>E:</strong> no (\alpha), no one ((=\text{all} \rightarrow \neg\text{some}))</td>
<td>never ((=\text{always} \rightarrow))</td>
<td>neither (of them) ((=\text{both} \rightarrow \neg\text{either}))</td>
<td>neither…nor ((=[\text{both} \rightarrow \text{and}] \rightarrow)</td>
<td>nor ((=\text{and} \rightarrow))</td>
</tr>
<tr>
<td><strong>O:</strong> *nall (\alpha), *never everyone ((=\text{some} \rightarrow \neg\text{all})) *nalways ((=\neg\text{always})) *noth (of them) ((=\neg\text{either} \rightarrow \neg\text{both})) *noth…nand ((=[\text{either} \rightarrow \neg\text{both}] \rightarrow)) *nand ((=\neg\text{and} \rightarrow))</td>
<td></td>
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As argued more fully elsewhere (Horn 1972; Horn 1989: §4.5), the motivation for this asymmetry is pragmatic: the relation of mutual non-logical inference between the positive and negative subcontraries results in the superfluity of one of these subcontraries for lexical realization; given the functional markedness of negation (see Horn 1989 for a comprehensive review), the superfluous, unlexicalized subcontrary will always be O.

We shall see below that the missing O phenomenon extends to the modals and deontics, and is also reflected in the general tendency toward O>E drift, wherein lexical items or collocations associated by their compositional form or etymology with the O corner of the square move inevitably northward toward E. But we will first elaborate the nature of the asymmetry
among the quantifiers and related adverbs and connectives in (8), where its operation is particularly robust.

This effect is especially striking when it overcomes morphology and etymology. Thus consider the Old English lexical item *nalles, nealles, which appears to challenge the constraint blocking *nall-type determiners, but is in fact attested only with the value ‘no, not, not at all’, never ‘not all’. Other OE quantificational expressions include *nafre ‘never’, *nædor ‘neither, nor’, *náht ‘nothing’, *nán ‘no one, none’, and *náhwar ‘nowhere’, all occupying the northeast E rather than the southeast O slot. Along the same lines, Jaspers (2005: 150) points to the Dutch adverb *nimmer – literally ‘nalways’, but actually denoting ‘never’.

We move now to the binary connectives, which have been situated on the Square since the medievals –cf. Ashworth (1974: 148, 167). Eloquent testimony to the persistent cross-linguistic exclusion of *nand is provided by the Latin neque, which exhibits the *nalles effect: its O morphology (‘not’ + ‘and’) belies its E (‘and not’) semantics, i.e. ‘neither, nor’ (Jaspers 2005: 150). While the nand gate, widespread in electronic circuitry, does indeed cover precisely the taboo O vertex, this merely underlines the absence of any such lexical item from natural languages. (But see Seuren 2006: fn. 8 for a potential counterexample.)

The modern English connective nor is essentially an E value, but it is usually restricted to negative polarity contexts –although an untriggered nor is not quite as restricted or marginalized as sometimes claimed, as in this passage:

The two values standardly lexicalized occupy the A and I slots, represented in English by and and or respectively. If a third position is represented, typically through negative incorporation, it maps onto the E vertex. Jespersen (1917: 108) cites Old English (and Old Norse) ne: as a negative phrasal conjunction ‘looking before and after’, so that *suð ne norð in Beowulf stands for ‘neither south nor north’. German offers a (rarely invoked) modern equivalent: in Wasser noch in Luft ‘neither in the water nor in the air’. (Horn 1989: 256)

But in fact similar occurrences of a Janus-faced nor are attested in both literary and colloquial English:3

3 The first two examples are cited in the OED, while the last three were provided by Arnold Zwicky and Beverly Flanigan in a thread on this topic on the ADS-L listserv. Other examples can be found by googling <“you nor anyone else” – neither>.
(10) **1872 TENNYSON** Great brother, thou nor I have made the world. [OED]
1954 W. FAULKNER A world such as caesar nor sultan nor khan ever saw [OED]
“Kent Smith, nor anyone from that office was present”
“I, nor my management, have ever had any kind of problem with creating a gay character.”
“I, nor my host, nor my file server, nor my ISP are responsible for what you do with the patches and ROM images found on this site.”

Crucially, while joint denial (p ↓ q, or in bit notation, <0001>) may be lexicalized, the Sheffer stroke (p | q, <0111>) cannot be. But what of exclusive disjunction, <0110>, occupying the Y position in the hexagon in (10)?

(11) **Figure 6**

\[
\begin{array}{c}
\text{<0110> (iff) } U (= A \lor E) \\
\text{p ↔ q} \\
\text{<1000> (and) A} \\
\text{p \land q} \\
\text{<1110> (or) I} \\
\text{p \lor q} \\
\text{<0111> (*and) O} \\
\text{p | q} \\
\text{<0100> (*xor) Y (= I \land O)} \\
\text{p @ q}
\end{array}
\]
In fact, true exclusive disjunction does exist—just not in natural language. As defined in set-theoretic terms, \( x \in A \text{xor} B \iff x \in A \cup B \land x \in A \cap B \). But no bona fide representatives of the exclusive disjunction operator have surfaced in natural language (Horn 1972, 1989; Gazdar & Pullum 1976; Jennings 1994; Katzir & Singh to appear).

There are, to be sure, pretenders to the throne. While Collinson (1937), Quine (1940), Geach (1972), and even Blanché (1969: 145) assert or presuppose that Lat. *aut* plays exclusive (Y) to *vel*’s inclusive (I)4, and while similar claims are made about Finnish or Welsh, closer inspection shows it just ain’t so (Horn 1989: 224–26). For example, Latin *aut*—the motivation for my @ (‘a(u)t’) notation for exclusive disjunction—was employed to oppose two mutually exclusive conditions (= ‘p or q, it matters which’), while *vel*—the source of the standard inclusive \( \lor \) connective—was used in free choice contexts (‘p or q, it doesn’t matter which’). *Aut aut*, damned “ambiguity”!

The pragmatic approach to so-called exclusive disjunction (Horn 1972, 1989) was prefigured in Archbishop Whately’s comments on the two disjuncts in e.g. *Virtue tends to procure us either the esteem of mankind or the favor of God* and in the more general (and still apt) considerations of Mill:

> [F]rom one being affirmed we are not authorized to deny the other. Of course, we are left to conjecture in each case, from the context, whether it is to be implied that the members are or are not exclusive.
> (Whately 1848: 106, emphasis added)

> When we say A is either B or C we imply that it cannot be both…If we assert that a man who has acted in a particular way must be either a knave or a fool, we by no means assert, or intend to assert, that he cannot be both.
> (Mill 1867: 512)

On the neo-Gricean account, *nand* (and *xor*) will be excluded for the same reason as *nall*: given that \( p \text{ or } q \) tends to implicate ‘[for all S knows] not both p and q’, the closed set of connectives need admit just the one \( \lor \) vertex disjunctive connective.

The asymmetry of (9) extends from the quantificational operators and connectives to other values that can be assigned a logical geometry. Consider, for example, the arithmetical (in)equalities, adjectival comparatives,

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4 Here, for example, is Quine (1940: 5) on the “ambiguity”: “We must decide whether ‘or’ is to be construed in an exclusive sense, corresponding to the Latin ‘aut’, or in an inclusive sense, corresponding to the Latin ‘vel’.”
and equatives in (12) (cf. Sesmat 1951: 319 ff. on the relation of these to other values on the hexagon of opposition):

(12)

While the A, E, and I values have an unrestricted distribution (Chris can be taller than, shorter than, or as tall as Robin regardless of their respective heights), the use of the O value (e.g., Chris is as short as Robin presupposes that Chris and Robin are (relatively) short. Earl may be as tall as Muggsy even if they’re both unusually short for their comparison set, but Shaq can’t be as short as Yao if they’re both 7-footers, given the marked nature of the “negative” adjective.

The lexicalization asymmetry of the Square extends to the modals and deontic operators (cf. van der Auwera 1996, Béziau 2003), as illustrated by the fact that the inflected negative in (13b) only allows wide scope (E
vertex) negation, i.e. the Roman Catholic reading, while its unlexicalized counterpart in (13a) allows both wide-scope (Catholic) and narrow-scope (Episcopalian) readings of the negation, the O version brought out by interpolation as in (14).\footnote{Note that despite the standard dictionary entry for cannot in which it is equated to ‘can not’, the former –as a lexicalization –can only get the E reading, never the O, regardless of whether the modal is interpreted as an alethic, root, or deontic operator.}

(13) a. A priest can not marry. \[¬◊(E) or ◊¬(O)]
   b. A priest {can’t/cannot marry}. \[only ¬◊(E), not ◊¬(O)]

(14) A priest can {always/if he wishes/of course} not marry.

The same asymmetry holds for could not, although it only shows up in the inflected form, since there is no *couldnot orthographic lexicalization alongside cannot:

(15) a. You could not work hard and still pass. \[¬◊(E) or ◊¬(O)]
   b. You couldn’t work hard and still pass. \[only ¬◊(E), not ◊¬(O)]

As with the quantifiers and binary connectives, it is the relation between the modal subcontraries (that of mutual implicature, even if we cannot accept Aristotle’s apparent equivalence between them: “whatever may walk…may not walk” –De Int. 21b12) that results in the resistance of the negative (O) subcontrary to lexicalization.

What of A-vertex modals? Must and should, whether understood logically, epistemically, or deontically, can only incorporate an inner negation, resulting in an E (or, in the case of should, E-like) meaning:

(16) a. You mustn’t go. = ‘you must [not go] \[□¬(E), not □¬(O)]
   b. You shouldn’t go. = ‘you should [not go] \[basically □¬(E)]

To be sure, the A modal need yields a lexicalized O value, as in (17a), but given the negative polarity status of need as a modal auxiliary (cf. (17b,c)), negation must scope over □ (need), ruling out the E reading. (Analogous distributional constraints hold for Dutch hoeven and Ger. brauchen.)
(17) a. She needn’t go.  = ‘not [she need go]’ [only $\neg\Box(O)$]
b. She {needs to/*need} go.
c. %Need you go? [% indicates dialectal variation in acceptability]

Thus, for example, (17’a) with modal need has unambiguously wide scope negation, while its non-modal counterpart in (17’b) takes narrow scope negation.

(17’) a. He need not leave.   [–$\Box$]  
b. He needs to not leave.  [–$\Box$]

It should also be noted that needn’t is restricted by semantics (it tends to be deontic) and register (it tends to be constrained to high or written style).

In some languages, including Turkish, ASL (American Sign Language), and LSF (Langue signée française), we find an opaque E-valued modal negation that is synchronically unrelated to possibility or necessity (cf. Shaffer 2002); the corresponding O form ($\approx$ need not) is semantically transparent and indeed non-lexicalized.

As we see from (17) vs. (13)-(16), while the asymmetry in lexicalizing complexes associated with the A, I, and sometimes E vertices as against O is equally exhibited across lexical domains, some domains are more equal than others (cf. van der Auwera 2001 for related discussion). The degree of asymmetry varies according to how closed the category is: strongest for connectives (*nand) and determiners/quantifiers (*nall, *nevery, *noth, *nalways), somewhat weaker for modal auxiliaries (where needn’t would violate the strong form of the constraint, albeit in a context in which no E reading would be possible), and weaker still (though still present) for ordinary adjectives (cf. impossible vs. unnecessary, where the latter but not the former is restricted to deontic, non-logical contexts). The motivation for this difference in the strength of the lexicalization constraints between closed and open category items is an important one, as an anonymous referee

6 Note also the asymmetry in nominalization potential (*unnecessity along side impossibility) and in cross-linguistic parallels (Lat. *innessarius, Fr. *innéssaire vs. impossibile, impossible). Similar asymmetries are found in the cross-linguistic expression of modality. Tamil veeNam may offer an instance of a lexicalized O verb (de Haan 1997: 80), but the facts are more complicated than de Haan suggests (E. Annamalai, p.c.). I hope to address this issue in later work.
points out, but it is one I cannot address here due to both space limitations and the speculative nature of any suggestions I could advance.

What we find in the open-class categories are implicational (rather than absolute) universals. First, the existence of a lexicalized $O$ form implies the existence of a lexicalized $E$ counterpart but not vice versa. Second, the lexicalized $E$ form tends to be more opaque and less constrained (semantically and distributionally) than the lexicalized $O$ form (if any). There are also clear differences in number. For example, among English causative verbs incorporating negation, the many verbs in (18a) contrast with the two in (18b):

(18) a. [CAUSE [E]]: ‘cause to become not {possible/legal/moral}’
   ban enjoin interdict proscribe
   bar exclude preclude refuse
deter forbid prevent veto
   disallow inhibit prohibit withhold

   b. [CAUSE [O]]: ‘cause to become not {necessary/obligatory},
      ‘{possible/legal/moral} not…’
      excuse exempt

Among the deontics, we have simplex nominal and adjectival realizations for the $A$ (obligation; obligatory/required), $I$ (permission; permitted/allowed), and $E$ values (prohibition; forbidden), but the $O$ values can only be complex (non-obligation, released from obligation,…). Among the adjectives, we do have $O$ candidates like optional, Fr. facultatif, or Ger. erübrigen, but it’s often unclear whether a particular modal (whether root, epistemic, or deontic) candidate occupies the $O$ or the $Y$ slot.7

The asymmetry of the Square also extends to “intermediate” values, south of $A/E$ but north of $I/O$, where ‘not many’ can be lexicalized (≈ few) but ‘many not’ cannot, ‘not often/usually not’ can be lexicalized (≈ seldom, rarely) but ‘often not/not usually’ cannot, etc. What is the appropriate generalization? To represent the intermediate values we exploit the fact that the quantifiers, quantificational adverbs, and modal values form scales as defined by unilateral entailment (Horn 1972, following Grice 1989). (In

7 This is a more general problem. Thus, Löbner (1990: 89) nominates a number of potential instances for “Typ 4” ($O$) lexicalizations in German (cf. also Löbner 1987), but on closer inspection several of these nominees (unnötig, fraglich, bezweifeln) are either limited to deontic uses or allow non-$O$ understandings.
these diagrams, $p$ represents an arbitrary proposition containing the scalar value in question and the subscripts indicate variation in strength as determined by unilateral entailment in non-monotone decreasing contexts.

(19)

Two terms in any quantitative opposition occupy different positions on a single scale, while two terms in a qualitative opposition will occupy parallel positions (weak, intermediate, or strong) on the corresponding scale. Plotting each scalar value according to its lower bound in the usual way and assigning positive and negative arithmetic values to those positions, we obtain this Arithmeticized Square (Horn 1989: 236 ff.)
Note that the cardinal values (A E / I O) are the strongest/weakest values on their respective scales and the sum of the values of any horizontal pair of quantificational determiners <Q, Q¬>, whether contraries or subcontraries, is always 0.\(^8\)

The crucial factor for determining whether an intermediate value can incorporate an inner or outer negation is where that value is situated with respect to the midpoint of its scale. This is codified by the notion of (in)tolerance (Löbner 1987: 64): “A quantifier Q is tolerant iff Q(P) and Q(~P) is possible at the same time. A quantifier is intolerant iff Q(P) excludes Q(~P)”. Given quantity scales like those in (21),

\[(21) \quad \langle \text{all, most, many, some} \rangle \quad \langle \text{no/none, few/not many, not all} \rangle \]
\[\langle \text{always, usually, often, sometimes} \rangle \quad \langle \text{never, rarely/seldom, not always} \rangle \]
\[\langle \text{(both…) and, (either…) or} \rangle \quad \langle \text{neither…nor, not both} \rangle \]
\[\langle \text{certain, likely, possible} \rangle \quad \langle \text{impossible, unlikely, not certain} \rangle \]
\[\langle \text{must, should/ought to, can/may} \rangle \quad \langle \text{can’t/mustn’t, shouldn’t, needn’t} \rangle \]

\(8\)  For elaboration, see Horn (1989: 237) and the addenda on pp.xxxiii-xxxiv of Horn (2001).
we can assign the values to the respective positive and negative scalar positions, and obtain the generalizations in (22), as illustrated in (23):

(22) \(<Q, Q\neg>\) are contraries if \(Q > .5\) and subcontraries if \(Q \leq .5\).

If \(Q \leq .5\), the conjunction \(Q \ldots and Q\neg\ldots\) is consistent, and \(Q\) is tolerant.

If \(Q > .5\), the conjunction \(Q\ldots and Q\neg\ldots\) is inconsistent, and \(Q\) is intolerant.

(23) a. Some of my friends are linguists and some of them aren’t.

Many of my friends are linguists and many of them aren’t.

He often goes to church on Sunday and he often doesn’t.

It’s possible that she’ll win, and possible that she won’t.

It’s 50-50 that it’ll land heads, and 50-50 that it won’t.

b. #All of my friends are linguists and all of them aren’t.

#Most of my friends are linguists and most of them aren’t.

#He usually goes to church on Sunday and he usually doesn’t.

#It’s likely that it’ll land heads, and likely that it won’t.

#It’s certain that she’ll win, and certain that she won’t.

The key principles of lexicalization (Horn 1972) can now be given as follows:

– When \(Q\) is intolerant, it may lexically incorporate its (contrary) inner negation \((Q_I\neg)\) but it tends not to lexicalize its outer negation \((\neg Q_I)\).

– A tolerant value may incorporate its outer negation \((\neg Q_T)\) but bars lexicalization of its inner negation \((Q_T\neg)\).

Thus, seldom or rarely lexicalize the inner negation of the intolerant usually (or the outer negation of the tolerant often), but there can be no simple lexical realization of not usually (or often not); similarly for few (= not many), a minority (= a majority…not), or unlikely (= likely…not).

The effect of these universals is to facilitate the direct expression of contrariety in natural language while blocking the direct expression of subcontrariety. Another reflection of this contrast is the strengthening of sentential (contradictory) negation to express a contrary meaning. In the words of Bosanquet (1911: 281), “The essence of formal negation is to invest the
contrary with the character of the contradictory”. The result is a variety of cases of contrary negatives in contradictory clothing (Horn 1989: Chapter 5). Some examples from English appear in (24):

(24) a. contrary readings for affixal negation (conventionalized strengthening)
   He is unhappy  
   She was unfriendly  
   I disliked the movie  

   (unilaterally entails ¬[He is happy])
   (unilaterally entails ¬[She was friendly])
   (unilaterally entails ¬[I liked the movie])

b. litotes/understatement in simple denials (online or non-convention-alized strengthening)
   He’s not happy with it
   I don’t like ouzo
   I’m not optimistic that φ

   (approaches ‘He’s unhappy with it’)
   (approaches ‘I dislike ouzo’)
   (approaches ‘I’m pessimistic that φ’)

c. “neg-raising” effects (strengthened understanding as a convention of usage)
   I don’t believe it’ll snow
   I don’t want you to go
   It’s not likely they’ll win

   (≈ I believe it won’t snow)
   (≈ I want you not to go)
   (≈ It’s likely they won’t win)

In each case, the negation of an unmarked “mid-scalar” positive scalar predication (at least) implicates a stronger, contrary negation.

Consider in particular the phenomenon of “neg-raising” in (24c), a tendency first recognized by St. Anselm (1033–1109), who pointed out that “we say non debet peccare [lit., ‘s/he NEG should sin’] when we mean debet non peccare” (Henry 1967: 193–94; cf. Hopkins 1972: 233–34). But which predicates license this lower-clause understanding of higher-clause negation? In general, neg-raising licensers are weak intolerant positive operators, situated just above the midpoint of the relevant scale (Horn 1989: §5.2). Their intolerance is demonstrated by plugging the NR predicates into the frame of (23):

(23’) a. #You should marry and you should not-marry.
   b. #I believe it will snow and I believe it won’t snow.
Weak intolerant positive predicates allowing NR readings contrast with tolerant, strong, and/or morphologically negative predicates that block them. Thus NR is licensed by:

\begin{align*}
& (25) \text{ believe, suppose but not know, doubt, disbelieve} \\
& \quad \text{ want, suggest but not insist, forbid, prohibit} \\
& \quad \text{ advisable, desirable but not obligatory, forbidden} \\
& \quad \text{ should, ought to, better but not have to, must, can} \\
& \quad \text{ likely, probable but not certain, impossible} \\
& \quad \text{ most but not all, many, some, few} \\
& \quad \text{ usually but not always, often, sometimes, rarely}
\end{align*}

As has often been noted, neg-raising functions euphemistically to tone down the expression of negative judgment, a motivation for litotes as well. In addition, as seen in the examples in (25), the weak-intolerance generalization crosscuts the traditional distinction between “lexical” and “functional” operators, as exemplified by the appearance of main verbs, modal auxiliaries, adjectives, determiners, and quantificational adverbs among the neg-raisers, provided they fit the scalar requirement.

A systematic exception to the weak intolerance is the class of strongly intolerant (A-position) deontic values, whose members often exhibit neg-raising effects. One classic example is the Fr. \textit{Il ne faut pas que tu meures} (lit., ‘it is not necessary that you die’, but usually = ‘you mustn’t die’). This example is described in the eponymous paper by Tobler (1882), who notes that the notoriously “unlogisch” placement of negation was attested by the 14th century alongside the “logical” \(O\) reading that it eventually comes to evict or block. Another instance of \(O\rangle E\) drift is provided by the strengthening of negated causatives. Thus while It. \textit{fare} + infinitive on its own conveys a strong causative (‘make’, not ‘let’), its negation is often understood with an \(E\)-style strengthened meaning:

\begin{align*}
& (26) \text{ Il caffè non mi fa dormire. ‘Coffee doesn’t {make/let} me sleep’}
\end{align*}

Not only in Italian but in such languages as Japanese, Turkish, Amharic, Czech, Biblical Hebrew, and Jacaltec, the negation of a strong causative (lit., ‘not make’) may or must strengthen to yield contrary (‘make not’ = ‘not let’ = \(E\)) force. The reverse drift, in which a ‘not let’ (\(E\)) causative is understood as ‘let not’ or ‘not make’ (\(O\)), on the other hand, appears to be unattested.
Further instances of the preferential treatment of E over O values are listed in (27), the first one having already been touched on.

(27)  


b. the opacity of E forms (*no*, *nary a*; Ger. *nie*; Fr. *personne*, *rien*, *jamais*)

c. the frequent difficulty of negating A modals without subsequent drift, e.g.

   You are to leave the room.  \(\text{(A)}\)
   You are not to leave the room.  \(\text{(E)}\)

d. an invariant E readings for complex adjectives with negation + possibility, e.g. \[\text{un-}[\text{V} \text{[-able]]} = \text{‘incapable of being Ved’ (E), ≠ ‘capable of not being Ved’ (O)}\]

e. complex adverbs incorporating semantics of I (*enough*) or E (*too*) but not O

f. the existence of “able” polarity and “unable” polarity vs. the non-existence of “needn’t” polarity

Thus, the apparent negated universal sequences in (27a) have an E meaning instead of the expected O. Other lexical instances of O>E drift include English *not at all* (cf. the undrifted *not altogether*) and French *pas du tout*. The basic, unanalyzable status characteristic of E forms is exemplified in (27b); *nary* – etymologically a reduction of *ne’er a* – is now entirely opaque, while the results of Jespersen’s Cycle in French exhibit little trace of their history as positive indefinites that have incorporated negative force (Latin *persona*, *rem*, *jam magis* respectively). No O values display this degree of semantic opacity. The superficial contradictory negation of A values often yield E results rather than the expected O, another example of induced contrariety (O>E drift), as seen in the quasi-modal pair in (27c). When negation combines with a possibility modal within a single lexical item, the result is virtually always an E rather than O meaning, with negation taking wide scope; an unreadable book is one that cannot be read rather than one that can be not read. Complement-taking adverbs may incorporate I-style (‘possible’) semantics (*tall enough = ‘so tall that ◊’) or E-style (‘impossible’)

\[\text{Van der Auwera (2001: 41) mentions additional candidates for this status, including Bengali *nēt*.}\]
semantics (too short = ‘so short that ¬◊’) but not O-style semantics (*shmoo short = ‘so short that ◊¬’). And as discussed in detail in Horn 1972: Chapter 3, alongside the instances of “able” or “possible” polarity (see (28a)) and “unable” or “impossible” polarity (see (28b)), items whose distribution is restricted to contexts of c-commanding I and E modality respectively, there is no attested “needn’t” polarity with the distribution of blarf in (28c).

(28) a. I can (*must, *needn’t) finally {afford a new car/tell them apart}.  
   It’s possible for me to {afford a new car/tell them apart}.  
  b. I couldn’t {fathom/make heads or tails of} the proposal.  
   I’m incapable of {fathoming/making heads or tails of} the proposal.  
  c. You needn’t (*can’t, *must) blarf that avocado.  
   It’s unnecessary (*possible/*impossible) for you to blarf that avocado.

Finally, we touch on one last asymmetry. When the neg-raising effect yields a strengthened E-type understanding alongside the literal O-type reading we often find that lexical incorporation of the negation renders the quasi-O readings inaccessible. Thus:

(29) a. It’s {not probable/not likely} that a fair coin will land heads.  
   (ambiguous; true on outer [contradictory] reading of negation)  
  b. It’s {improbable/unlikely} that a fair coin will land heads.  
   (unambiguously inner [contrary] negation, hence false)

(30) a. It’s not likely that Federer will win and not likely that he’ll lose.  
   (allows tolerant, contradictory reading with outer negation)  
  b. #It’s unlikely that Federer will win and unlikely that he’ll lose.  
   (allows only intolerant [neg-raised], hence anomalous reading)

(31) a. It’s not {advisable/desirable} that you go there alone.  
   (ambiguous)  
  b. It’s {inadvisable/undesirable} that you go there alone.  
   (only a warning not to)

In each case, as with can’t or couldn’t, it is the lexicalization in the (b) cases that forces the contrary E readings and blocks the contradictory O reading, while both are available in the corresponding non-lexicalized sequences in
the (a) counterparts. We could also point to such minimal oppositions as *disprove and *disbelieve on the one hand, with \(A \neg = E\) analyses, as against *disallow and *disable, with \(\neg I = E\) analyses.\(^{10}\)

The first neo-Gricean account of the asymmetries discussed in this study appeared in Horn (1972), although additional data have been accumulated since. (See in particular the cross-linguistic data surveyed in Horn 1989: §4.5 and the arguments in Jaspers that partially support and partially challenge those analyses.) No natural language instances of *nall or *nand have yet surfaced. In many, probably most, languages, neither of the negative positions (E or O) is lexicalized. But the generalization remains sound: A, I, and often E values may lexicalize, O values may not. On the proposed account, the three-cornered square is a consequence of the maxim of Quantity: in any situation in which I possess (and am known to possess) complete knowledge, and in which that knowledge is (and is known to be) relevant to you, I can convey that information to you via a proposition containing one of the three values all, some (implicating some not, not all), or none. The fourth value (*nall = not all, implicating some) is functionally (although not logically) expendable.

Over the succeeding decades, others have offered their own translations of the story of *O. Huybregts’ (1979) blocking principle stipulates that not \(Q\) can lexicalize just when \(Q \neg\) can’t, but this correlation fails to fully explain just when the latter state of affairs obtains. The monotonicity correspondence universal of Barwise & Cooper (1981: 186–87) predicts inter alia that strong determiners like every or most can incorporate inner but not outer negation; this correctly allows neither and no while ruling out *nevery and *noth. But without a grounding in the pragmatics of scalar operators, such approaches to the constraints on quantifier lexicalization are ad hoc. Worse still, any treatment based on the semantics of the determiners and quantifiers like that of Barwise & Cooper (1981) fails to generalize to the binary connectives, modals, and other non-quantificational values, much less to the intermediate values. A later proposal along similar lines is that of Hoeksema (1999), who, after reviewing earlier accounts, argues that the non-occurring O forms are not blocked by corresponding I forms.

\(^{10}\) Further support for the preference for contrary readings in natural language is surveyed in Horn (2008), which includes a closer look at “neg-raising” and related cases of negative strengthening and explores the phenomenon of “virtual contrariety” in cases of double negations that don’t quite cancel out.
pace Horn (1972). Rather, he notes, neither of the likely sources that would yield lexicalized O quantifiers—the merger of an existential value + negation or the reinterpretation of NPIs—is consistent with what is known of the plausible historical development. Once again, however, the considerations he raises, contributing factors though they may be, fail to extend to other scalar values that manifest an asymmetry in lexicalization.

More recently, Seuren (2003: 13) has advanced a new formalization of the Aristotelian Predicate Calculus on which A, I, and (sometimes) A* (= E) will have lexicalized representations but I* (the O of the standard square) does not. He argues that, contra the Gricean moral to the story I have drawn, “The question [of why there is no *nall] is superfluous…an artifact of the defective way [the Aristotelian Predicate Calculus] was formalized by Boethius” and the other geometers of the Square. But altering the representation does not explain the asymmetry in the lexical incorporation of negation.11

One more approach to the lexicalization asymmetries is worth reviewing briefly here. Moeschler (2007, 2009) disputes the neo-Gricean line of Horn 1972, 1989 on these asymmetries. Like those of Huybregts and Hoeksema, Moeschler’s critique is flawed by his exclusive concentration on the quantificational values, ignoring the related asymmetries among the binary connectives, modals, and other operators that can be mapped on the Square, along with the extension of the asymmetries to the intermediate values. In addition, Moeschler (2007: 4) refutes a straw argument from “complexity” that I have never made; indeed, on complexity grounds alone, there is no way to choose between E and O, since each is equally complex in combining negation with quantification or modality. Yet in each of the relevant cases, the O values are more likely to resist lexicalization or direct expression than their E counterparts, as the neo-Gricean generalization predicts.

While Moeschler (2007: 5) asserts that “according to Horn, utterances whose truth-conditions are different (I and O) have identical Q-implicatures”, the claim is actually that they have complementary Q-implicatures in that the assertion of either will (ceteris paribus) implicate that (for all the speaker knows) the other holds; asserting some F are G implicates that (for all the speaker knows) not all F are G, and vice versa. But it is not

11 I must defer any response to the nuanced critiques of Jaspers 2005 and Seuren 2006 for another occasion.
the case that “I and O both implicate the conjunction of I and O.” In fact, the Y-vertex proposition that some but not all F are G is not claimed to be directly implicated by either an I or O proposition, but may be communicated by what is said together with what is implicated. Nor can Q-implicatures be “just truth-conditional logical implications” (cf. Moeschler 2007: 11), given their cancelability.\[12\]

Finally, I am not sure what to make of the argument that the implicature-based account should be jettisoned for one invoking the relevance-theoretic notion of explicature on the grounds that “the theory of scalar implicatures is outdated.” As will be confirmed by even a quick review of the contents of leading journals, lists of conference and workshop announcements, and recent work like that of Geurts (2009, to appear), this death-knell is untenable as either a theoretical conclusion or a fashion statement.

In sum, we draw this moral from \textit{L'Histoire d’*O}: The relation of mutual quantity implicature holding between positive and negative subcontraries I and O results in the superfluity of one of the two for lexical realization, while the functional markedness of negation allows us to predict that the unlexicalized subcontrary will always be O rather than I. The pragmatic account of the asymmetries built into the “three-cornered square” is more general and more explanatory than rival theories that either dismiss the asymmetry as uninteresting or restrict it to the determiners and quantificational operators while ignoring its relevance to lexicalized negation with other operator types (binary connectives, modals, adverbs, predicates) and the intermediate values that can be mapped onto the Square of Opposition.

\[12\] On the claim that “negative particulars do not trigger Q-implicatures or scalar implicatures” (Moeschler 2007: 11), a position also maintained by Chierchia (2004), see Horn (2009: §3) for a detailed response.
Acknowledgments

Earlier versions of some of this material were presented in Berkeley (1970), Austin (1973), Milan (2003), Lansing (2003), and New York (2004). I am indebted to those who attended those presentations, to the participants in the Montreux congress, and to Barbara Abbott, Elayaperumal Annamalai, Jack Hoeksema, Polly Jacobson, Dany Jaspers, Jacques Moeschler, Hans Smessaert, Rashad Ullah, Victor Sánchez Valencia, Raffaella Zanuttini, Arnold Zwicky, and especially the two anonymous referees. Needless to say,…

References


Tobler, A. (1882). Il ne faut pas que tu meures “du darfst nicht sterben’’.
_Vermischte Beiträge zur französischen Grammatik 1_, (3rd ed.), 201–05.
Leipzig: S. Hirzel.


